Arthur Jaffe's Papers

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References

- Complex Angular Momentum in Two-Channel Problems, with Y.S. Kim, *Phys. Rev.*, 127 (1962), 2261–2266.
- [2] Asymptotic Behavior of the S Matrix for High Angular Momentum, with Y.S. Kim, *Phys. Rev.*, **129** (1963), 2818–2823.
- [3] Divergence of Perturbation Theory for Bosons, Commun. Math. Phys., 1 (1965), 127–149.
- [4] Entire Functions of the Free Field, Ann. Phys. (N.Y.), **32** (1965), 127–156.
- [5] Nonpositivity of the Energy Density in Quantized Field Theories, with H. Epstein and V. Glaser, Nuovo Cimento, 36 (1965), 1016–1022.
- [6] On the Approximation of Quantum Field Theories, J. Math. Phys., 6 (1965), 1172–1178.
- [7] Dynamics of a Cut-off $\lambda \phi^4$ Field Theory, Princeton University Thesis (1965).
- [8] Existence Theorems for a Cut-off $\lambda \phi^4$ Field Theory, in *Mathematical Theory of Elementary Particles*, R. Goodman and I. Segal (eds.), MIT Press (1966).
- [9] Local Quantum Fields at Operator-Valued Generalized Functions, in *Conference on Dispersion Theory at MIT*, I.E. Segal (ed.), MIT (1966).
- [10] A Preliminary Study of Infinite Volume Limits in a Cut-off $\lambda \phi^4$ Field Theory, Conference on Functional Integration and Constructive Quantum Field Theory, Editor, I.E. Segal, MIT (1966).
- [11] Wick Polynomials at a Fixed Time, J. Math. Phys., 7 (1966), 1250–1255.
- [12] Form Factors at Large Momentum Transfer, Phys. Rev. Lett., 17 (1966), 661–663.
- [13] High Energy Behavior of Local Quantum Fields, SLAC PUB 250 (1966), Stanford Linear Accelerator Center.
- [14] A Generalization of the Paley-Wiener-Schwartz Theorem, SIAM Review, 15 (1967), 1046– 1047.
- [15] High Energy Behavior in Quantum Field Theory. I. Strictly Localizable Fields, *Phys. Rev.*, 158 (1967), 1454–1461.

- [16] A Yukawa Interaction in Infinite Volume, with J. Glimm, Commun. Math. Phys., 11 (1968), 9–18.
- [17] Constructive Quantum Field Theory, with K. Osterwalder, ETH Lectures, Zürich, (1968).
- [18] Infinite Volume Limit of a $\lambda \phi^4$ Field Theory, with R. T. Powers, Commun. Math. Phys., 7 (1968), 218–221.
- [19] A $\lambda \phi^4$ Quantum Field Theory without Cut-offs. I, with J. Glimm, *Phys. Rev.*, **176** (1968), 1945–1961.
- [20] A Model of Yukawa Quantum Field Theory, with J. Glimm, Phys. Rev. Letters, 23 (1969), 1362–1365.
- [21] Progress in Constructive Field Theory, in Contemporary Physics, Vol. II Editor, A. Salam, International Atomic Energy Agency, Vienna (1969).
- [22] Singular Perturbations of Selfadjoint Operators, with J. Glimm, Comm. Pure and Applied Math., 22 (1969), 401–414.
- [23] A General Class of Cut-off Model Field Theories, with O.E. Lanford and A.S. Wightman, Commun. Math. Phys., 15 (1969), 47–68.
- [24] Constructing a $\lambda(\phi^4)_2$ Quantum Theory, pp. 120–151, in *Local Quantum Theory*, Editor, R. Jost, Academic Press (1969).
- [25] Strictly Localizable Fields, in *Meeting on Renormalization*, Editor, A. Salam, Trieste, (1969).
- [26] Renormalization of Hamiltonians, in *Meeting on Renormalization*, Editor A. Salam, Trieste, (1969).
- [27] Whither Axiomatic Field Theory?, Reviews of Modern Physics, 41 (1969), 576–580.
- [28] An Infinite Renormalization of the Hamiltonian is Necessary, with J. Glimm, Jour. Math. Phys., 10 (1969), 2213–2214.
- [29] Model Estimates and Results, in Proc. of the CNRS International Colloquium on Systems with an Infinite Number of Degrees of Freedom, D. Ruelle and L. Michel (eds.), Paris, CNRS, (1970).
- [30] Relativistic Covariance of an Interacting Quantum Field, with John T. Cannon, Bull. Am. Math. Soc., 76 (1970), 853–855.
- [31] Progress in Quantum Field Theory, in Proceedings of the 1970 Kiev Conference on High Energy Physics, pp. 618–632, Editor, V. Shelest, Naukova Dumka, Kiev (1971).

- [32] Lorentz Covariance of the $\lambda(\phi^4)_2$ Quantum Field Theory, with J. Cannon, Commun. Math. Phys., **17** (1970), 261–321.
- [33] Rigorous Quantum Field Theory Models, with J. Glimm, Bull. Am. Math. Soc., 76 (1970), 407–410.
- [34] The $\lambda(\phi^4)_2$ Quantum Field Theory without Cut-offs: II. The Field Operators and the Approximate Vacuum, with J. Glimm, Ann. of Math., **91** (1970), 362–401.
- [35] Relativistic Covariance of an Interacting Quantum Field, with J. Glimm, Bull. Am. Math. Soc., 76 (1970), 853–357.
- [36] Self-Adjointness of the Yukawa₂ Hamiltonian, with J. Glimm, Annals of Physics (N.Y.), 60 (1970), 321–383.
- [37] The $\lambda(\phi^4)_2$ Quantum Field Theory without Cut-offs. III. The Physical Vacuum, with J. Glimm, Acta Math. **125** (1970), 203–267.
- [38] Energy-Momentum Spectrum and Vacuum Expectation Values in Quantum Field Theory, with J. Glimm, Jour. Math. Phys., 11 (1970), 3335–3338.
- [39] The Energy-Momentum Spectrum and Vacuum Expectation Values in Quantum Field Theory, II. with J. Glimm, Commun. Math. Phys. 22 (1971), 1–22.
- [40] Positivity and Self Adjointness of the $P(\phi)_2$ Hamiltonian, with J. Glimm, Commun. Math. Phys., **22** (1971), 253–258.
- [41] Quantum Field Theory Models, with J. Glimm, in *Statistical Mechanics*, C. DeWitt and R. Stora (eds.) Gordon and Breach Science Publishers, New York (1971).
- [42] The Yukawa₂ Quantum Field Theory without Cut-offs, with J. Glimm, Jour. Funct. Anal., 7 (1971), 323–357.
- [43] Boson Quantum Field Models, with J. Glimm, in *Mathematics of Contemporary Physics*, Editor, R. Streater, Academic Press, 1972.
- [44] The $\lambda(\phi^4)_2$ Quantum Field Theory without Cut-offs. IV. Perturbations of the Hamiltonian, with J. Glimm, Jour. Math. Phys., **13** (1972), 1568–1584.
- [45] Constructive Field Theory, Phase II, in Fundamental Interactions in Physics and Astrophysics, Plenum Press, New York, (1973).
- [46] What is Renormalization?, with J. Glimm, pp. 401–411 in Partial Differential Equations, a symposium held at the Univ. California, Berkeley, California 1971, and published as Proc. Sympos. Pure Math. Vol. XXIII, American Mathematical Society, Providence, Rhode Island, (1973).

- [47] Positivity of the ϕ_3^4 Hamiltonian, with J. Glimm, Fortschritte der Physik, **21** (1973), 327–376.
- [48] The Particle Structure of the Weakly Coupled $P(\phi)_2$ Model and Other Applications of High Temperature Expansions, Part I: Physics of Quantum Field Models, with J. Glimm and T. Spencer, in *Constructive Quantum Field Theory*, Editor, A.S. Wightman, Springer Lecture Notes in Physics Volume 25, (1973).
- [49] The Particle Structure of the Weakly Coupled $P(\phi)_2$ Model and Other Applications of High Temperature Expansions, Part II: The Cluster Expansion, with J. Glimm and T. Spencer, in *Constructive Quantum Field Theory*, Editor, A.S. Wightman, Springer Lecture Notes in Physics Volume 25, (1973).
- [50] The Particle Search in a Quantum Field Model, with J. Glimm, Bull. Am. Math. Soc., 79 (1973), 979–980.
- [51] The *n*-Particle Cluster Expansion for the $P(\phi)_2$ Quantum Field Model, with J. Glimm, unpublished.
- [52] What Constructive Field Theory Says About Currents, with O. McBryan, in *Local Currents and Their Applications*, Editors, D.H. Sharp and A.S. Wightman, pp. 19–30 (1974), North Holland Publishing Company (1974).
- [53] Status of Constructive Field Theory, in Proceedings of the 17th International Conference on High Energy Physics, J.R. Smith (ed.), pages I243–I250 London (1974).
- [54] The Entropy Principle for Vertex Functions in Quantum Field Models, with J. Glimm, Ann. de l'Inst. Henri Poincaré A21 (1974), 1–26.
- [55] Critical Point Dominance in Quantum Field Models, with J. Glimm, Ann. de l'Inst. Henri Poincaré A21 (1974), 27–41.
- [56] ϕ_2^4 Quantum Field Model in the Single-Phase Region: Differentiability of the Mass and Bounds on Critical Exponents, with J. Glimm, *Phys. Rev.*, **D10** (1975), 536–539.
- [57] Remark on the Existence of ϕ_4^4 , with J. Glimm, Phys. Rev. Lett., **33** (1974), 440–442.
- [58] The Wightman Axioms and Particle Structure in the $P(\phi)_2$ Quantum Field Model, with J. Glimm and T. Spencer, Ann. of Math., 100 (1974), 585–632.
- [59] Phase Transitions for ϕ_2^4 Quantum Fields, with J. Glimm and T. Spencer, Commun. Math. Phys., 45 (1975), 203–216.
- [60] Absolute Bounds on Vertices and Couplings, with J. Glimm, Ann. de l'Inst. Henri Poincaré A22 (1975), 97–107.

- [61] On the Approach to the Critical Point, with J. Glimm, Ann. de l'Inst. Henri Poincaré, A22 (1975), 109–122.
- [62] Two- and Three-Body Equations in Quantum Field Models, with J. Glimm, Commun. Math. Phys., 44 (1975), 293–320.
- [63] Three particle structure of ϕ^4 interactions and the scaling limit, with J. Glimm, *Phys. Rev.* **D11** (1975), 2816–2827.
- [64] Particles and Bound States and Progress Toward Unitarity and Scaling, with J. Glimm, in Mathematical Problems in Theoretical Physics, H. Araki, (ed.) Springer Lecture Notes in Physics (1976).
- [65] Mathematical Problems Motivated by Quantum Field Theory, in C* Algebras and their Applications to Physics, S. Doplicher, (ed.) Academic Press (1976).
- [66] ϕ^j Bounds in $P(\phi)_2$ Quantum Field Models, with J. Glimm, in *Mathematical Methods of Quantum Field Theory*, F. Guerra, D. Robinson, and R. Stora (eds.) CNRS (1976).
- [67] Critical Problems in Quantum Fields, with J. Glimm, in Mathematical Methods of Quantum Field Theory, Editors, F. Guerra, D. Robinson, and R. Stora, CNRS (1976).
- [68] Existence of Phase Transitions for ϕ_2^4 Quantum Fields, with J. Glimm and T. Spencer, in *Mathematical Methods of Quantum Field Theory*, Editors, F. Guerra, D. Robinson, and R. Stora, CNRS (1976).
- [69] Problèmes Ergodiques dans la Théorie Quantique des Champs, Astérisque, 40 (1976), 105– 112.
- [70] Critical Exponents and Renormalization in the ϕ^4 Scaling Limit, with J. Glimm, Acta Physica Austriaca 16 (1976), 147–166.
- [71] An Asymptotic Perturbation Expansion for Multiphase ϕ_2^4 , with J. Glimm and T. Spencer, Acta Physica Austriaca, 16 (1976), 167–175.
- [72] A Convergent Expansion about Mean Field Theory, Part I. The Expansion, with J. Glimm and T. Spencer, Ann. Phys. 101 (1976), 610–630.
- [73] A Convergent Expansion about Mean Field Theory, Part II. Convergence of the Expansion, with J. Glimm and T. Spencer, Ann. Phys. 101 (1976), 631–669.
- [74] Particles and Scaling for Lattice Fields and Ising Models, with J. Glimm, Commun. Math. Phys. 51 (1976), 1–13.
- [75] Phase Transitions in P(φ)₂ Quantum Fields, with J. Glimm and T. Spencer, Bull. American Mathematical Society, 82 (1976), 713–715.

- [76] Critical Exponents and Elementary Particles, with J. Glimm, Commun. Math. Phys., 52 (1977), 203–209.
- [77] Review of "Introduction to Axiomatic Quantum Field Theory" by N.N. Bogolubov, A.A. Logunov, and I.T. Todorov, in Bull. Amer. Math. Soc. 83 (1977), 349–351.
- [78] Quark Trapping for Lattice U(1) Gauge Fields, with J. Glimm, *Physics Letters*, **66B** (1977), 67–69.
- [79] A Tutorial Course in Constructive Field Theory, with J. Glimm, in New Developments in Quantum Field Theory and Statistical Mechanics, Editors, M. Lévy, P. Mitter, Plenum Press (1977).
- [80] Functional Integral Methods in Quantum Field Theory, with J. Glimm, in New Developments in Quantum Field Theory and Statistical Mechanics, Editors, M. Lévy, P. Mitter, Plenum Press (1977).
- [81] Instantons in an U(1) Lattice Gauge Theory: A Coulomb Dipole Gas, with J. Glimm, Commun. Math. Phys., 56 (1977), 195–212.
- [82] Lattice Instantons: What Are They and Why Are They Important? in *Mathematical Problems in Physics*, Springer Lecture Notes in Physics, Editors, G.-F. Dell'Antonio, S. Doplicher, and G. Jona-Lasinio (1977).
- [83] Meron Pairs and Quark Confinement, with J. Glimm, *Phys. Rev. Letters*, **40** (1977), 277–278.
- [84] Multiple Meron Solutions of the Classical Yang-Mills Equation, with J. Glimm, *Physics Letters*, **73B** (1978), 167–170.
- [85] Droplet Model for Quark Confinement, with J. Glimm, Phys. Rev., D18 (1978), 463–467.
- [86] Probability Applied to Physics, with J. Glimm, Lecture Notes in Mathematics, Volume 2, University of Arkansas Press, Fayetteville (1978).
- [87] Introduction of Gauge Theories, in Proceedings of the International Congress of Mathematicians, Helsinki, Editor, O. Lehto, pp. 905–916 (1978).
- [88] Charges, Vortices and Confinement, with J. Glimm, Nucl. Phys. B149 (1979), 49–60.
- [89] The Resummation of One Particle Lines, with J. Glimm, Commun. Math. Phys., 67 (1979), 267–293.
- [90] A Note on Reflection Positivity, with J. Glimm, Lett. Math. Phys., 3 (1979), 377–378.
- [91] The Coupling Constant in a ϕ^4 Field Theory, with J. Glimm, in *Recent Developments in Gauge Theories*, Editors, G. 't Hooft, C. Itzykson, A. Jaffe, H. Lehmann, P.K. Mitter, I.M. Singer, R. Stora; Plenum Press (1980).

- [92] Classical Gauge Theories and Their Quantum Role, published in *Recent Developments in Gauge Theories*, Editors, G. 't Hooft, C. Itzykson, A. Jaffe, H. Lehmann, P.K. Mitter, I.M. Singer, R. Stora, Plenum Press (1980).
- [93] Vortices and Monopoles Structure of Static Gauge Theories, with C. Taubes, 290 pages Birkhäuser-Boston, Inc., (1980).
- [94] Constructive Field Theory, in Mathematical Problems of Theoretical Physics, Editor, K. Osterwalder, Springer Lecture Notes in Physics (1981).
- [95] Renormalization, in Seminar on Differential Geometry, S.-T. Yau (ed.) Annals of Mathematics Study 102, Princeton Press (1981).
- [96] Quantum Physics, with J. Glimm, Springer-Verlag, New York, 415 pages (1981).
- [97] Exact Renormalization Group for Gauge Theories, with T. Balaban and J. Imbrie, in *Progress in Gauge Field Theory*, pp. 79–103, Editors, H. Lehmann, G. 't Hooft, A. Jaffe, Plenum Publishing Corporation (1984).
- [98] The Mass Gap for Higgs Models on a Unit Lattice, with T. Balaban, D. Brydges and J. Imbrie, Annals of Physics 158 (1984), 281–319.
- [99] Ordering the Universe: the Role of Mathematics, in *Renewing U.S. Mathematics*, National Academy Press (1984). Reprinted in *SIAM Review* 26 (1984), 473–500, and in *Notices of the American Mathematical Society* 31 (1984), 589–608.
- [100] Renormalization of the Higgs Model: Minimizers, Propagators and the Stability of Mean Field Theory, with T. Balaban and J. Imbrie, *Commun. Math. Phys.*, 97 (1985), 299–329.
- [101] Euclidean Quantum Field Theory, Nucl. Phys., **B254** (1985), 31–43.
- [102] Expansions in Statistical Physics, with J. Glimm, Commun. Pure and Applied Math., 68 (1985), 613–630.
- [103] Collected Papers, Vol. I: Quantum Field Theory and Statistical Mechanics; Expositions, with J. Glimm, 418 pages, Birkhäuser Boston (1985).
- [104] Collected Papers, Vol. II: Constructive Quantum Field Theory, Selected Papers, with J. Glimm, 533 pages, Birkhäuser Boston (1985).
- [105] Constructive Gauge Theory, with T. Balaban, in Fundamental Problems of Gauge Field Theory, Editors, G. Velo and A. Wightman, Plenum Press (1986).
- [106] Quantum Physics, Second Edition, with J. Glimm, 535 pages, Springer-Verlag (1987).
- [107] Ground State Structure in Supersymmetric Quantum Mechanics, with A. Lesniewski and M. Lewenstein, Ann. Phys., 178 (1987), 313–329.

- [108] Index of a Family of Dirac Operators on Loop Space, with A. Lesniewski and J. Weitsman, Commun. Math. Phys., 112 (1987), 75–88.
- [109] Conversation between Arthur Jaffe and Klaus Peters, The Mathematical Intelligencer, 9, #4 (1987), 11–15.
- [110] The Two-Dimensional, N=2 Wess-Zumino Model on a Cylinder, with A. Lesniewski and J. Weitsman, Commun. Math. Phys., 114 (1988), 147–165.
- [111] Effective Action and Cluster Properties of the Abelian Higgs Model, with T. Balaban and J. Imbrie, Commun. Math. Phys., 114 (1988) 257–315.
- [112] A Priori Estimates for the N=2, Wess-Zumino Model on a Cylinder, with A. Lesniewski, Commun. Math. Phys., 114 (1988), 553–575.
- [113] The Loop Space $S^1 \to \mathbb{R}$ and Supersymmetric Quantum Fields, with A. Lesniewski, and J. Weitsman, Annals of Physics, **183** (1988), 337–351.
- [114] Quantum K-Theory, I. The Chern Character, with A. Lesniewski and K. Osterwalder, Commun. Math. Phys., 118 (1988), 1–14.
- [115] Heat Kernel Regularization and Infinite Dimensional Analysis, in Mathematical Quantum Field Theory and Related Topics Canadian Mathematical Proceedings Volume 9, Joel S. Feldman and Lon M. Rosen, Eds., American Mathematical Society: Providence, 1988.
- [116] Mathematics at the Heart of Science, Balomenos Lectures, University of New Hampshire Press, 1988.
- [117] On Convergence of Inverse Functions of Operators, with A. Lesniewski and K. Osterwalder, Jour. Funct. Anal. 81 (1988), 320–324.
- [118] Pfaffians on Hilbert Space, with A. Lesniewski and J. Weitsman, Jour. Funct. Anal., 83 (1989), 348–363.
- [119] Supersymmetric Field Theory and Infinite Dimensional Analysis, with A. Lesniewski, in Nonperturbative Quantum Field Theory, Proceedings of the 1987 Cargèse Summer School, G. 't Hooft et. al., Editors, Plenum Press 1988.
- [120] Supersymmetry and the Spectral Condition, with A. Lesniewski and C. Wieczerkowski, Lett. Math. Phys., 16 (1988), 385–388.
- [121] Heat Kernel Regularization of Quantum Fields, with A. Lesniewski and C. Wieczerkowski, Commun. Math. Phys., 121 (1989), 337–344.
- [122] A Priori Quantum Field Equations, with A. Lesniewski and C. Wieczerkowski, Annals of Physics, 192 (1989), 2–20.

- [123] Quantum K-Theory, II. Homotopy Invariance of the Chern Character, with K. Ernst, P. Feng, and A. Lesniewski, Jour. Funct. Anal., 90 (1990), 355–368.
- [124] On Super-KMS Functionals and Entire Cyclic Cohomology, A. Jaffe, A. Lesniewski, and K. Osterwalder, K-Theory, 2 (1989), 675–682.
- [125] Deformations of Super-KMS Functionals, with A. Lesniewski and M. Wisniowski, Commun. Math. Phys., 121 (1989), 527–540.
- [126] An Index Theorem for Super Derivations, with A. Lesniewski, Commun. Math. Phys., 125 (1989), 147–152.
- [127] Convergence of an Iterative Neural Network Learning Algorithm for Linearly Dependent Patterns, with Kenneth Berryman, Mario Inchiosa, and Steven Janowsky, J. Phys. A, 23 (1990), L223–L228.
- [128] Extending the Pseudoinverse Rule, with Kenneth Berryman, Mario Inchiosa, and Steven Janowsky, in *Neural Networks and Spin Glasses*, edited by K. Theumann and R. Koeberle, World Scientific, Singapore, 1990.
- [129] The Importance of Mathematics, SUNY Research, 9, 4–7 (1989).
- [130] The Heisenberg Algebra on a Riemann Surface, with A. Lesniewski and S. Klimek, Commun. Math. Phys., 126 (1989), 421–431.
- [131] Constructive Field Theory and Entire Cyclic Cohomology, Proceedings of the April 1989 Ringberg Conference, F. Hirzebruch, Editor.
- [132] Ward Identities for Non-Commutative Geometry, with K. Osterwalder, Commun. Math. Phys., 132 (1990), 119–130.
- [133] Geometry of Supersymmetry, with A. Lesniewski, in *Constructive Quantum Field Theory II*, (Erice, 1988), edited by A. Wightman and G. Velo, 283–305, NATO Adv. Sci. Inst. Ser. B Phys., 234, Plenum, New York, 1990.
- [134] Mathematics motivated by physics, Proceedings of Symposia in Pure and Applied Mathematics 50 (1990), 137–150, American Mathematical Society.
- [135] Asymptotically Commuting Families of Operators, with S. Klimek and A. Lesniewski, Comment. Math. Helvetici 65 (1990), 672–679.
- [136] The modular group and super-KMS functionals, with Orlin Stoytchev, in *Differential geo*metric methods in theoretical physics (Rapallo, 1990), 382–384, Lecture Notes in Phys., 375, Springer, Berlin, 1991.

- [137] Non-Commutative Geometry and Mathematical Physics, in New Symmetry Principles in Quantum Field Theory, J. Fröhlich, et. al., Editors, Plenum Press, 1992
- [138] Quantum Physics as Non-Commutative Geometry, in Mathematical Problems in Theoretical Physics, A. Uhlmann et. al. Editor, 281–290, Springer, Berlin, 1992.
- [139] Theoretical Mathematics: toward a cultural synthesis of mathematics and theoretical physics, with Frank Quinn, Bulletin of the American Mathematical Society, 29 (1993), 1–13. (Czech Translation by Pavel Exner. Pokroky Mat. Fyz. Astronom., 41 (1996), 25–37.
- [140] Huzihiro Araki, with Alain Connes, Moshé Flato, Heisuke Hironaka, and Vaughan Jones, Comm. Math. Phys. 155 (1993), 1–2.
- [141] Stability of a Class of Bi-Local Hamiltonians, with A. Lesniewski and K. Osterwalder, Commun. Math. Phys., 155 (1993), 183–197.
- [142] Round table: physics and mathematics. XIth International Congress of Mathematical Physics (Paris, 1994), 691–705, Internat. Press, Cambridge, MA, 1995.
- [143] University of Rochester Plan to Cut Mathematics Is Recipe for Disaster, with Joseph Lipman, and Morton Lowengrub, *Chronicle of Higher Education*, March 1, 1996, page B1.
- [144] Demotion of Mathematics meets groundswell of protest, with Salah Baouendi and Joseph Lipman, Notices of the Amer. Math. Soc., 43 (1996), 307-313.
- [145] Roland L. Dobrushin, with Joel Lebowitz and Ya. G. Sinai, Comm. Math. Phys., 189 (1997), 259–261.
- [146] Proof and the Evolution of Mathematics, Synthese, 111(1997), 133-146.
- [147] Reflection and Twists, in Les Relations Entre les Mathématiques et la Physique Théorique, Festschrift for the 40th Anniversary of the IHES, 119–130, September 1998.
- [148] Where does quantum field theory fit into the big picture? in Conceptual foundations of quantum field theory (Boston, MA, 1996), A. Cao, Editor, 136–147, Cambridge Univ. Press, Cambridge, 1999.
- [149] Quantum harmonic analysis and geometric invariants, Advances in Math. 143 (1999), 1–110.
- [150] Twist positivity, Ann. Phys. 278 (1999), 10–61.
- [151] The holonomy expansion, index theory, and approximate super-symmetry, Ann. Phys. 279 (2000), 161–262.
- [152] Quantum Invariants, Comm. Math. Phys. **209** (2000), 1–12.

- [153] Twist fields, the elliptic genus, and hidden symmetry, *Proc. Nat. Acad. Sci.*, **97** (2000), 1418–1422.
- [154] Twist fields and broken supersymmetry, with Olivier Grandjean, J. Math. Phys., 41 (2000), 3698-3763.
- [155] Constructive quantum field theory, in *Mathematical Physics 2000*, edited by T. Kibble, 111– 127, Imp. Coll. Press, London, 2000.
- [156] Twist Positivity for Lagrangian Symmetries, with Olivier Grandjean and Jon Tyson, Advances in Theoretical and Mathematical Physics, 4 (2000).
- [157] Equations for Universal Truth, *The Times Higher Educational Supplement*, July 28, 2000, London.
- [158] The elliptic genus and hidden symmetry, Commun. Math. Phys., 219 (2001), 89–124.
- [159] Derivatives with Twists, Reviews in Mathematical Physics, 14 (2002), 887–895.
- [160] Interactions between Mathematics and Theoretical Physics, in New Trends in the History and Philosophy of Mathematics, Tinne Hoff Kjeldsen and Lise Mariane Jeppesen, editors, University of Odense Press, 2003.
- [161] The Role of Rigorous Proof in Modern Mathematical Thinking, in New Trends in the History and Philosophy of Mathematics, Tinne Hoff Kjeldsen and Lise Mariane Jeppesen, editors, University of Odense Press, 2003.
- [162] An Exchange Identity for Non-Linear Fields, with Christian Jäkel, Comm. Math. Phys. 264 (2006), 283–289.
- [163] Quantum Yang-Mills Theory, with Edward Witten, in *Millennium Prize Problems*, American Mathematical Society, Providence, RI, 2006.
- [164] Introduction to Quantum Field Theory, Notes available at www.arthurjaffe.net
- [165] The Millennium Prize Problems, Introduction and Editor with J. Carlson and A. Wiles, American Mathematical Society, Providence, 2006.
- [166] The Millennium Grand Challenge in Mathematics, Notices of the American Mathematical Society, 53 (2006), 652–660.

- [167] Quantum Field Theory on Curved Backgrounds. I. The Euclidean Functional Integral, with Gordon Ritter, Comm. Math. Phys. 270 (2007), 545–572.
- [168] Mathematical Physics, Discussion at the Royal Irish Academy, with Michael Atiyah, Michael Berry, Luc Drury, and Arthur Jaffe, moderated by Brendan Goldsmith. Published Dublin, 2007.
- [169] Lunch with George, Notices of the American Mathematical Society, 53 (2007), 833–836.
- [170] Quantum Field Theory on Curved Backgrounds. II. Spacetime Symmetries, with Gordon Ritter, *Comm. Math. Phys.*, in press.
- [171] Reflection Positivity and Monotonicity, with Gordon Ritter, submitted for publication.
- [172] Replica Condensation and Tree Decay, with David Moser, preprint.
- [173] Constructive Jürg, A Personal Overview of Constructive Quantum Field Theory, Lecture at the E.T.H. Zurich on 3 July 2007, posted at http://www.arthurjaffe.com/Assets/pdf/ ETH-Juerg.pdf
- [174] Quantum Theory and Relativity, in *Contemporary Mathematics* Group Representations, Ergodic Theory, and Mathematical Physics: A Tribute to George W. Mackey, R. S. Doran, C.C. Moore, and R. J. Zimmer, Editors, 449 (2008) 209–246.